# Solar electrons in the Heliosphere 

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1. Galactic cosmic Rays (GCRs)
2. Anomalous cosmic rays (ACRs), that originate as interstellar neutral atoms traveling into the heliosphere, ionized by solar UV and carried out as pickup ions in the solar wind to be finally accelerated to energies as high as $100 \mathrm{MeV} /$ nucleon presumably close to the solar wind termination shock or in the heliosheath.

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1. Galactic cosmic Rays (GCRs)
2. Anomalous cosmic rays (ACRs)
3. Solar energetic particles (SEPs) that originate near the Sun in association with intense solar flares and large coronal mass ejections (CMEs). Occasionally, SEP events are observed at very high energies reaching GeV for protons and 100 MeV for electrons.

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4. Energetic particles accelerated by other shocks and disturbances in the solar wind such as shocks formed in the solar wind stream interaction regions (SIRs) or corotating interaction regions (CIRs).

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4. Particles accelerated by SIRs or CIRs
5. Energetic particles accelerated in planetary magnetospheres, such as Jovian electrons observed in the inner heliosphere at energies from a few hundred keV to less than about 30 MeV .

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The study of these particle populations at different latitudes and under different heliospheric conditions provides information about:

- the global structure of the heliosphere during solar minimum and solar maximum conditions
- the mechanisms of particle propagation in the heliosphere - properties of solar source regions (charge states, composition). Energetic particles given insight both on the heliosphere and on processes back at Sun.

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The intensities of all particle populations which propagate through the heliosphere are affected by

- variations in the level of solar activity,
- the characteristics of the solar wind,
- the properties of the interplanetary magnetic field

Changes in these properties result in

- short-term and long-term modulations of GCRs and ACRs,
- variations in latitudinal and radial gradients of particle intensities,
- and changes in the energy spectra and composition of the heliospheric energetic particle population.

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- Electron propagation
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- Pitch angle scattering
- In situ electrons observed near the Earth
- Inversion of observed electron profiles
- In-situ and hard x-rays
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Electrons from the Sun will propagate in the interplanetary magnetic field.
In the absence of large-scale disturbances like CMEs and shocks, the interplanetary magnetic field can be described as a smooth average field due to the steady solar wind flow.

The magnetic field in the solar wind is "frozen" in the plasma, and is carried by the solar wind flow.

The Sun rotates, so althongh the wind flowing from a given region in the corona propagates radially, the solar wind will have a spiral structure.

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With no solar wind effects included, particle propagation is based on the model of focused transport illustrated by the equation (Roelof, 1969)


- $z$ is the coordinate of the observer along the magnetic field line, $\mu$ is the cosine of pitch angle. $t$ the time. $v$ is the particle velocity
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The equation includes terms describing the streaming of particles along the field lines, and terms describing the change of the particles' pitch angles.

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## Magnetic field line

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## Problem

Consider $B \propto R^{-2}$
consider a particle at Venus with $\mu=-0.95$
at what distance will it sent hack?
what is the minimum $|\mu|$ for a particle, sent from Mars towards the Sun, to reach the orbit of Mercury?

Orhit of Mercury: 38700821 AU. Orbit of Mars: 1.52366231 AU.

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Particles are subject to small-angle scatterings off magnetic turbulence.
Kinetic approach (Kocharov 1998), parametrized by a mean free path $\lambda$, isotropic scattering, scattering centers frozen in the solar wind.

- a time step is chosen such that the particle only travels a very small fraction if $\lambda$
- anter each time step the position of the particle and its pitch angle are updated using only the effects of adiabatic focusing
- Particles $v$ and $\mu$ are then changed into solar wind frame of reference and scatter is added by performing small rotations in the particle velocity vector following Kocharov (1998), assuming constant radial mean free path).
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Focused transport with scattering.
Example:

- 50 electrons, with 100 keV , released from 3 Rs in ecliptic plane
- outward motion, initial $\mu$ uniform in $] 0,1[$
- spiral magnetic field (solar wind $400 \mathrm{~km} / \mathrm{s}$ )
- magnetic field intensity varying as $R^{-2}$
- constant mean free path $\lambda=1 \mathrm{AU}$

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200 keV electrons from EPAM/ACE. Long duration event, with anisotropic onset. Slow rise and long duration could be related to long-lasting injection at the Sun. Particles from anti-sunward direction at the onset suggest the reason is very strong scattering.


200 keV electrons from EPAM/ACE. Average pitch angle (anisotropy).

## Modeling propagation effects

Kinetic treatment: 1 million particles generated randomly. Solar wind effects included, adiabatic focusing and isotropic scatter (mean free path does not depend on the pitch angle).
for each $\lambda$ the injection function is determined (deconvolution not a fit)
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Data are enough to chose between the different models.
Mean free path is $\approx 0.045 \mathrm{AU}$.


Injection function peaks and drops relatively fast. It coincides with remote observations of gyro-synchrotron emissions. Ref: Maia et al (2007). ApJ 660:874-881.

