

SOLAR CORONAL HEATING: A HUNT FOR NANOFLARES

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OUTLINE

1. What is the solar corona?
2. The problem of solar coronal heating
3. The role of magnetic field and magnetic reconnection
4. Solar flares and “nanoflares”
5. Probing nanoflares with fluctuations of the coronal X-ray and EUV emission (in collaboration with S Tsuneta and Y Sakamoto, National Astronomical Observatory of Japan)



1999 eclipse, Turkey

A bit of history

1868 – helium spectral line discovered on the Sun

1869 – unknown green coronal emission line

→ a new element, "coronium" suggested

1895 – helium identified in laboratory

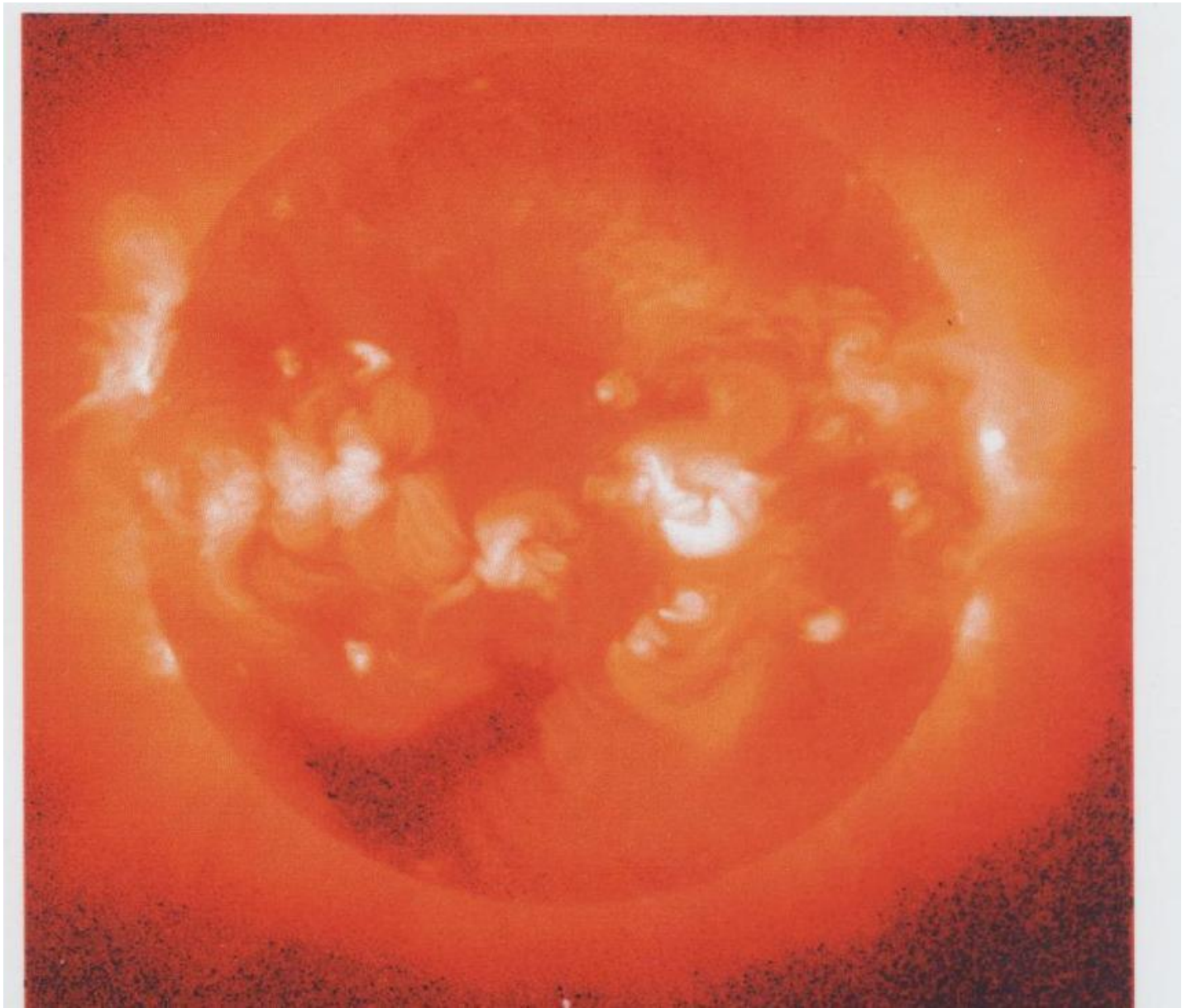
1939 – "coronium" spectral line identified as optical transition in the 13 times ionized iron

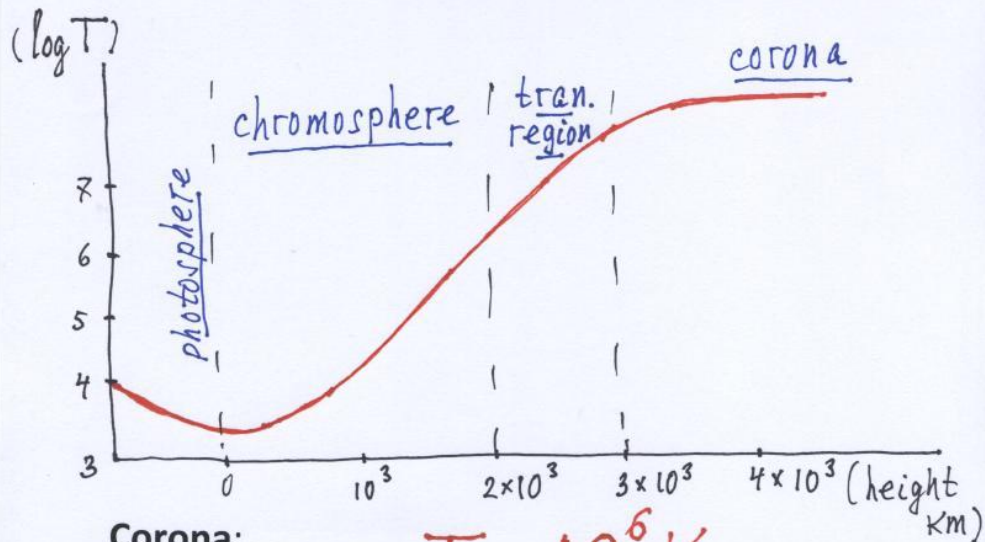


corona is very hot !



$$T_e > 10^6 K!!!$$





Corona:

$$T_c \sim 10^6 \text{ K}$$

$$n_c \sim (10^8 \div 10^9) \text{ cm}^{-3}$$

quiet Sun

active regions

Energy supply
required

$$q_c \text{ (erg/cm}^2\text{.s)}$$

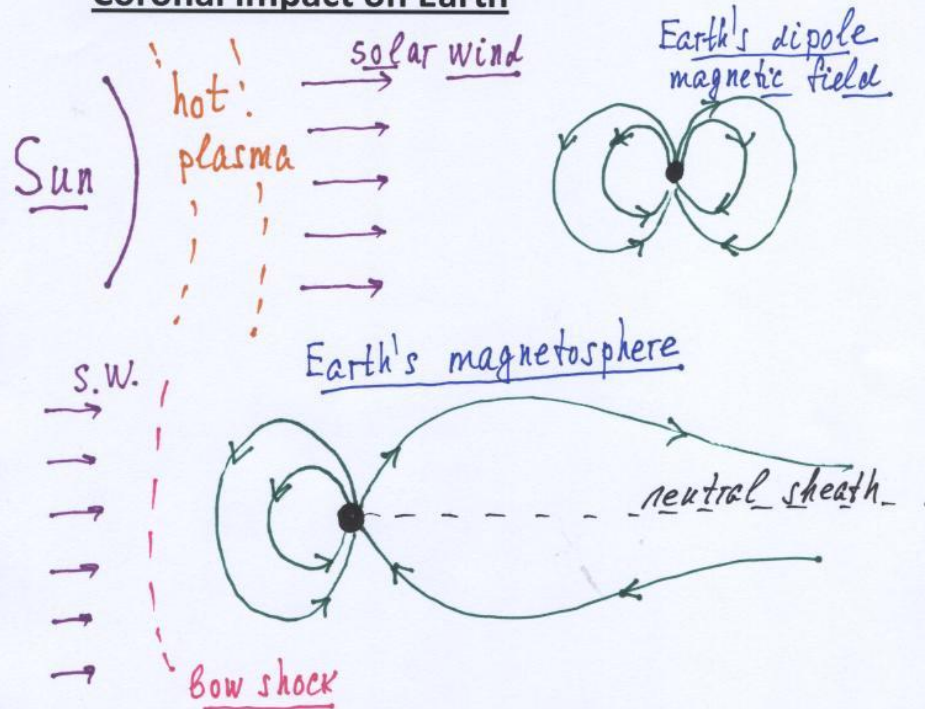
$$\rightarrow \sim 3 \times 10^5$$

$$\sim 10^7$$

Total solar luminosity:

$$q_{\odot} \approx 6.3 \times 10^{10} \text{ erg/cm}^2\text{.s}$$

Coronal impact on Earth



Variations in SW →

(solar flares,
coronal mass ejections,
etc...)

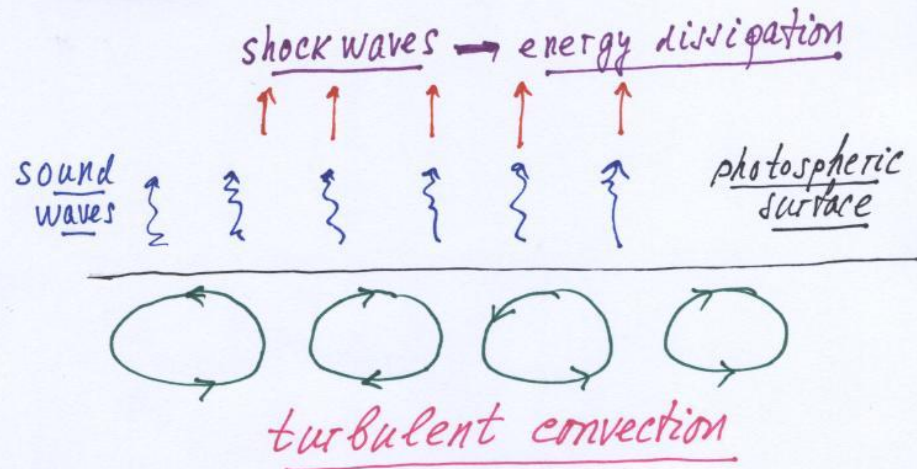
Magnetospheric

pulsations

(magnetic storms,
aurora, etc...)

SPACE WEATHER

"Old" theory of coronal heating: acoustic heating

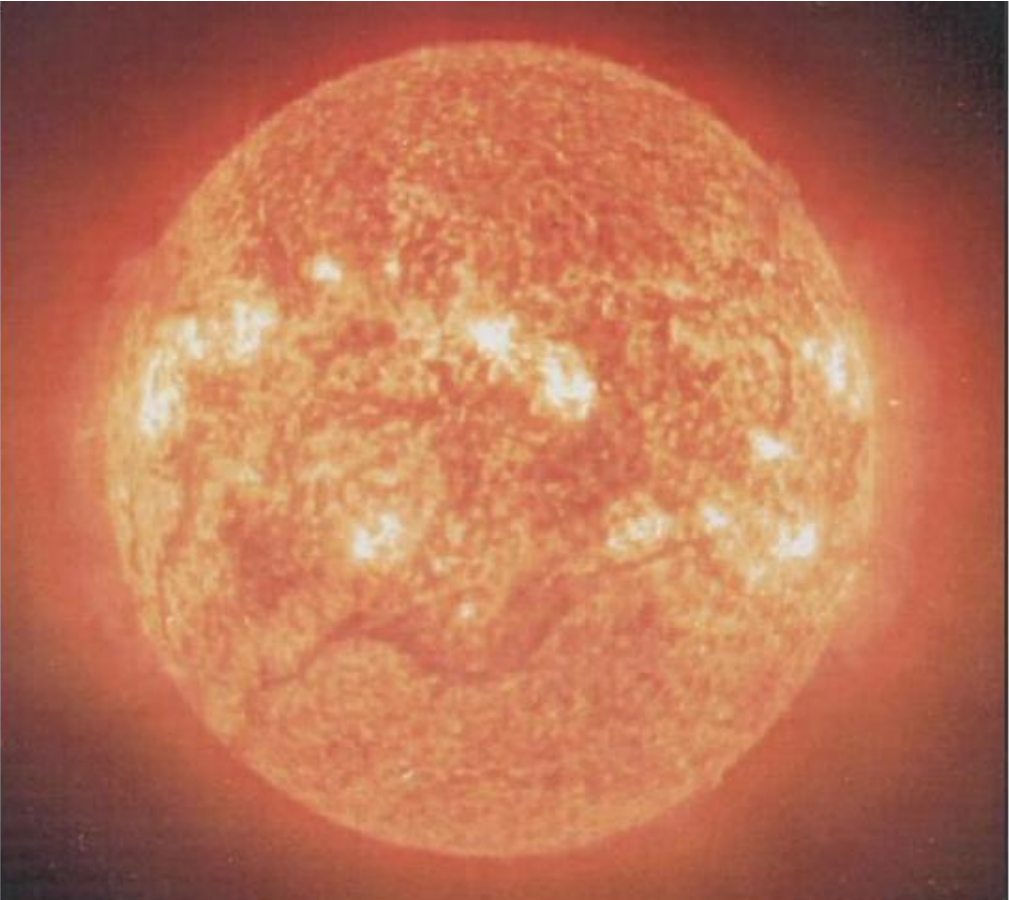
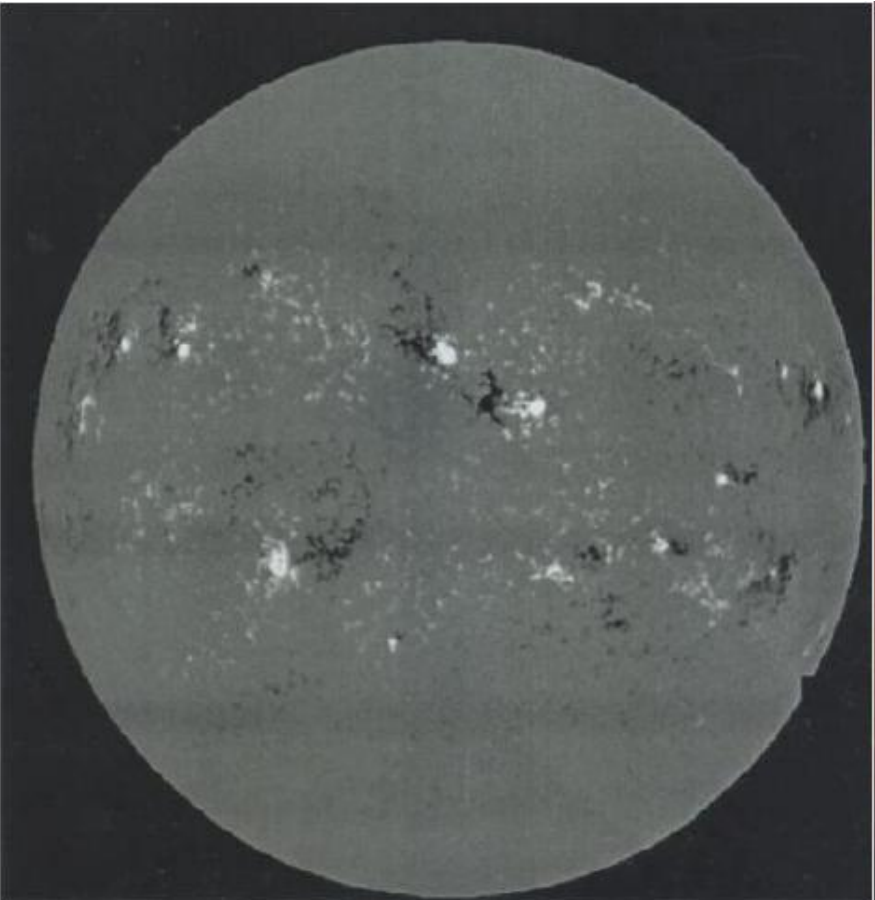


Main drawbacks

- i) Observed acoustic energy flux is too small
- ii) Strong correlation between the X-ray activity in the corona and the coronal magnetic field

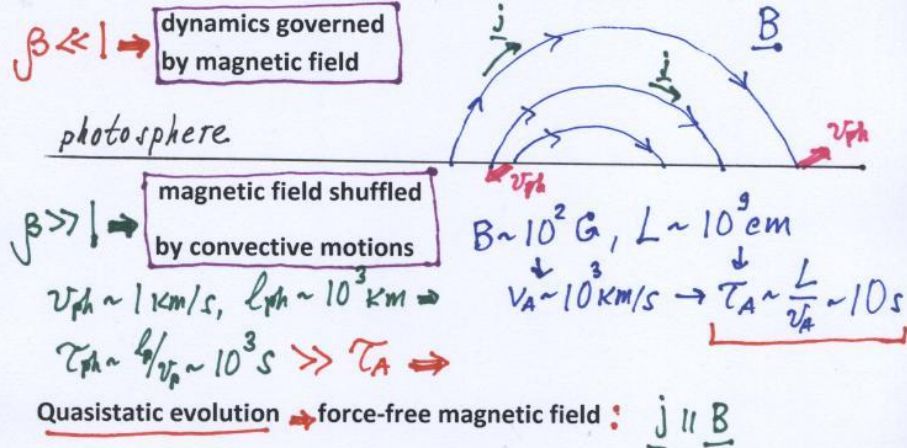


Magnetic nature of the solar coronal heating

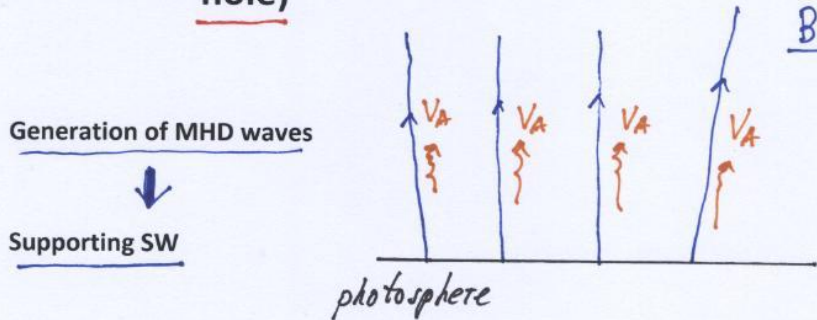


Magnetic coronal heating: how does it work?

i) active region magnetic loop



ii) open magnetic region (coronal hole)



Magnetic energy: a viable energy source

Injected power (Poynting flux)

$$P \sim v_{ph} \cdot B^2 / 4\pi$$

$$P_{max} \sim 10^8 \text{ erg/cm}^2 \cdot \text{s} \gg 9c$$

Major problem: extremely high electric conductivity of the coronal plasma

$$\sigma = \frac{ne^2 \tau_e}{m_e} \propto T_e^{3/2}$$

$$\text{Resistivity } \eta = \frac{1}{\mu_0 \sigma} \propto T_e^{-3/2}$$

Global Ohmic energy dissipation is completely irrelevant

$$\tau_{\Omega} \sim L^2 / \eta \equiv S \tau_A$$

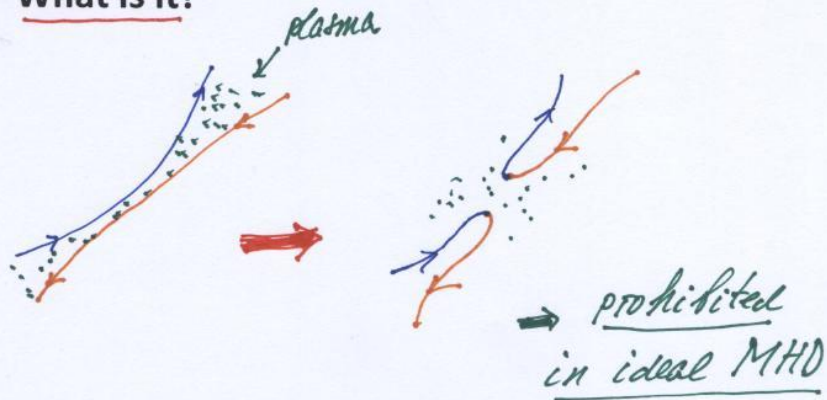
$$S \equiv \tau_e / \tau_A = \frac{L \cdot v_A}{\eta} - \text{Lundquist number}$$

$$S \sim 10^{12} \text{ for the corona} \Rightarrow \tau_{\Omega} \sim 10^6 \text{ years!!}$$

Possible way out \rightarrow magnetic energy release via magnetic reconnection

MAGNETIC RECONNECTION

What is it?



What is it for?

Magnetic energy release via reconnection is by far more effective than with the global Ohmic heating

$$\tau_r = \tau_A \cdot S_1^{\alpha}, \quad 0 < \alpha < 1$$

$$\alpha = \frac{1}{2} \rightarrow \text{classical Sweet-Parker reconnection model}$$

$$\alpha \rightarrow 0 \rightarrow \text{fast reconnection model}$$

$$\tau_r \sim 10^2 \tau_A$$

Reconnection events in the solar corona



Solar flares

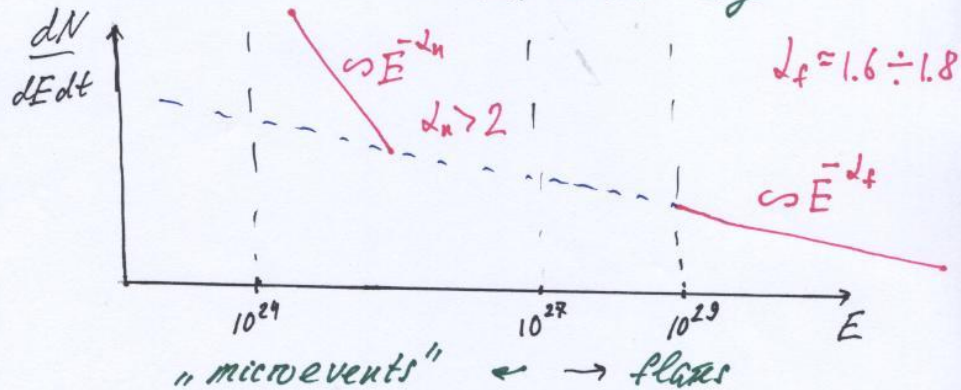
Energy range: $(10^{29} \div 10^{33}) \text{ erg} \rightarrow$

Not frequent enough for maintaining the hot corona



NANOFLARE concept (Parker, 1988) →

Corona is heated by numerous small flare-like reconnection events with $E_n \lesssim 10^{24} \text{ erg}$



the outcome is very sensitive to assumptions on the structure of emitting plasma as well as on the events selection procedure

How to test the nanoflare heating scenario

without being able to resolve individual nanoflares
observationally ?



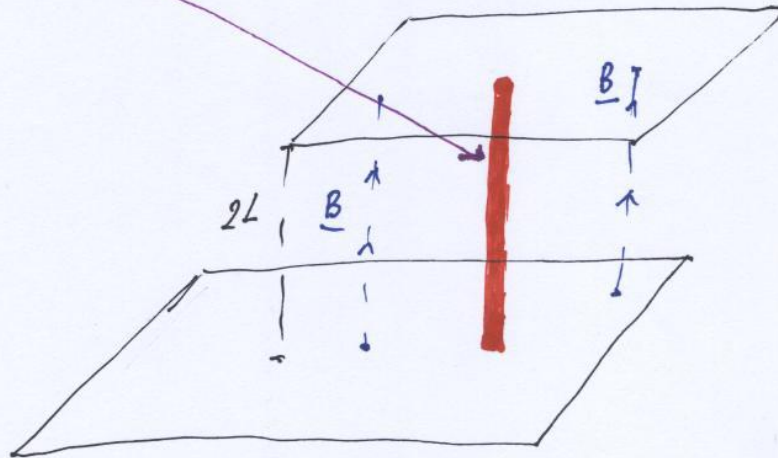
Forward modeling of the nanoflare-heated solar corona



Observable signature of the nanoflare heating

Each nanoflare →

A single hot coronal filament with $\beta \sim 1$





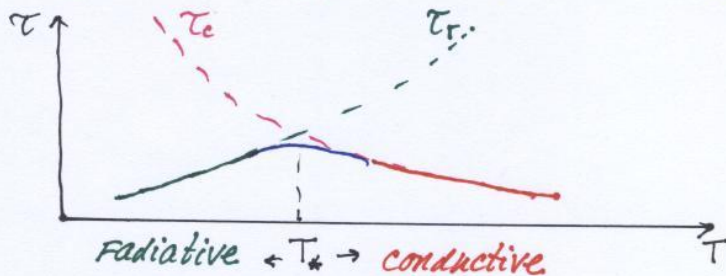
Cooling of the hot coronal filament

Heat conduction

$$\tau_c \approx 4 \times 10^{-10} n L^2 / T^{5/2}$$

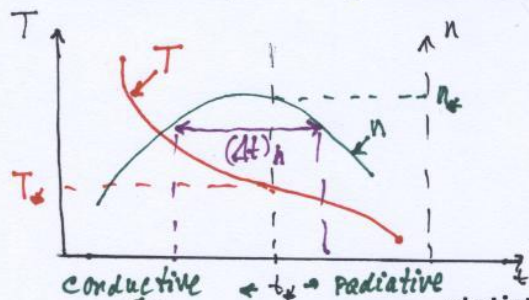
Radiation

$$\tau_r = 2 \times 10^{-3} T^{3/2} / n$$



Two-stage cooling process →

Conductive phase → Radiation phase



$$T_* \approx 4 \times 10^4 B^{2/3} L^{1/3}$$

$$n_* \approx 3.5 \times 10^{11} B^{1/3} L^{-1/3}$$

$$(\Delta t)_h \approx t_c \approx 10^{-4} L^{5/6} B^{-1/3}$$

$$B = 30 \text{ G}; L = 10^9 \text{ cm}$$

$$T_* \approx 4 \times 10^4 \text{ K}; n_* \approx 3 \times 10^{10} \text{ cm}^{-3}$$

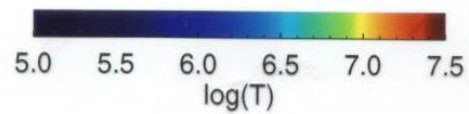
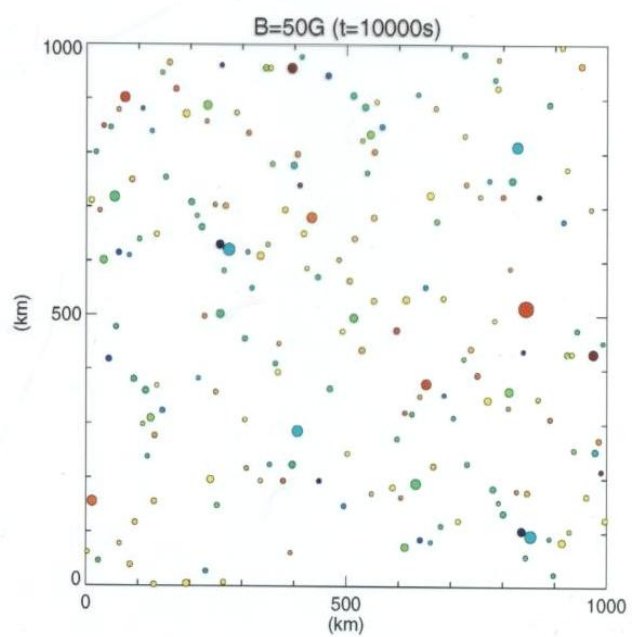
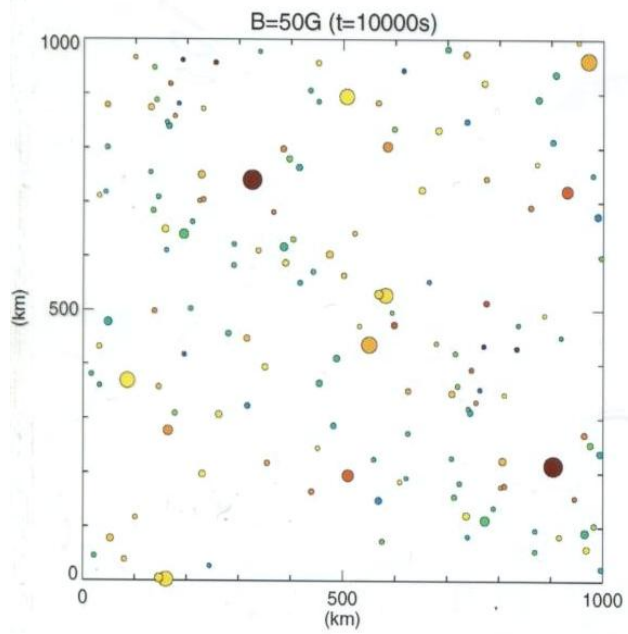
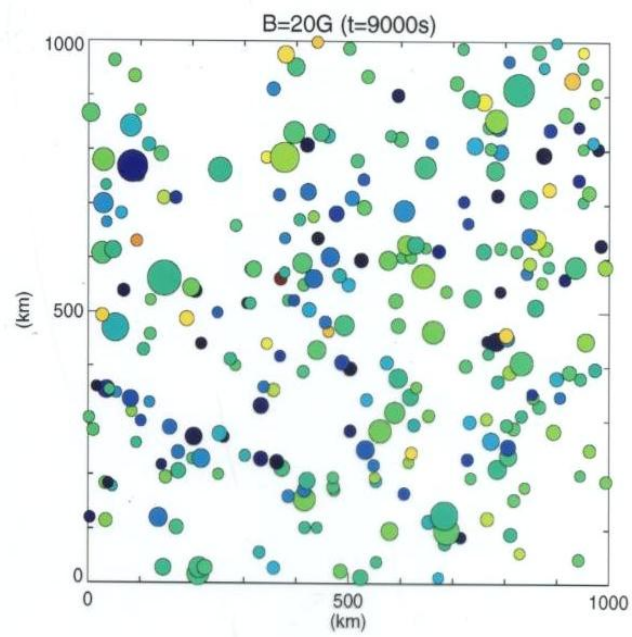
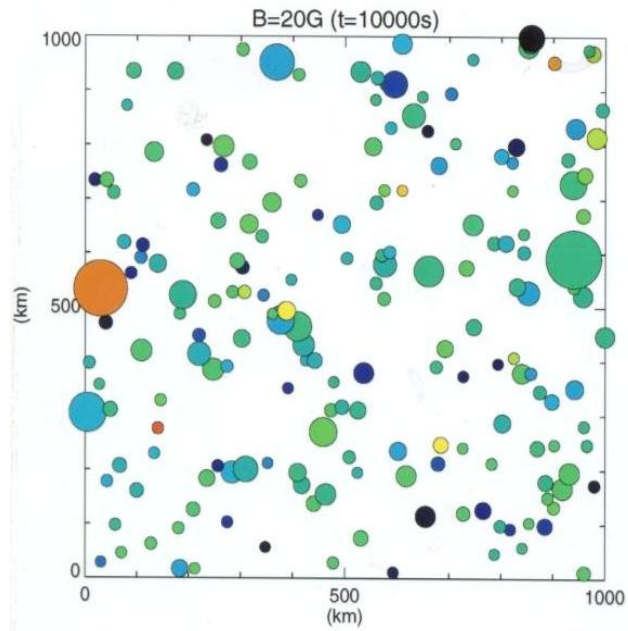
$$(\Delta t)_h \approx 10^3 \text{ s}$$

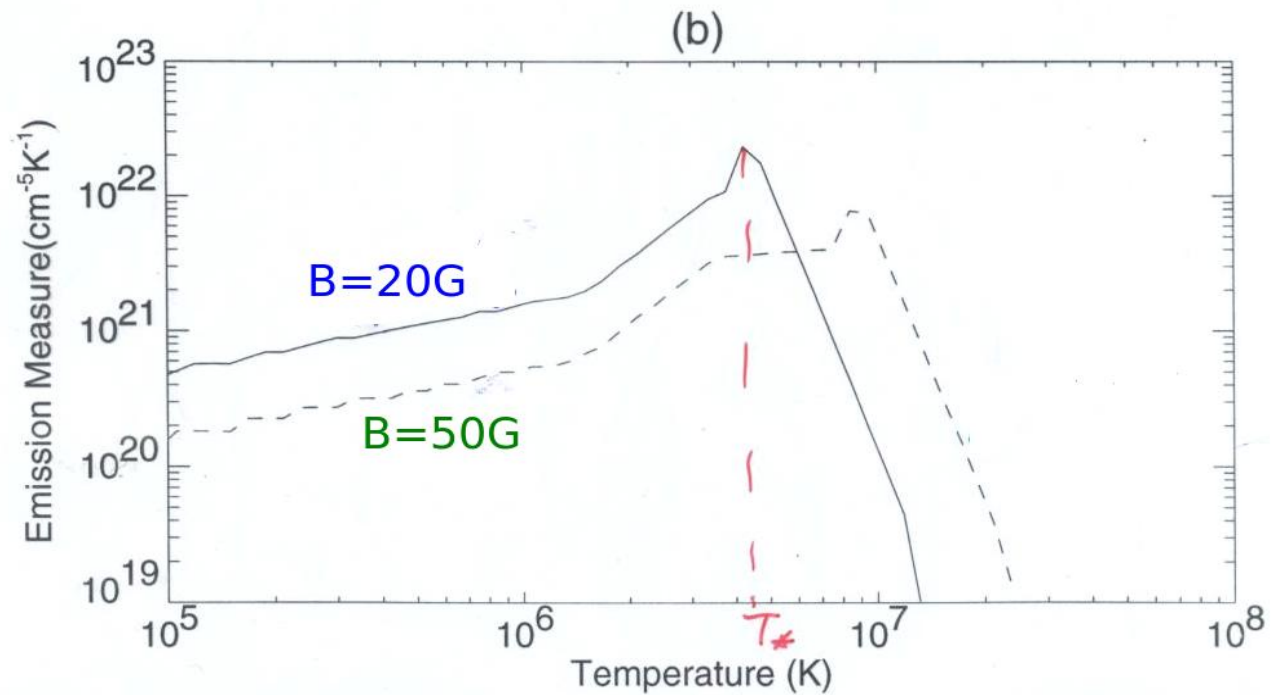
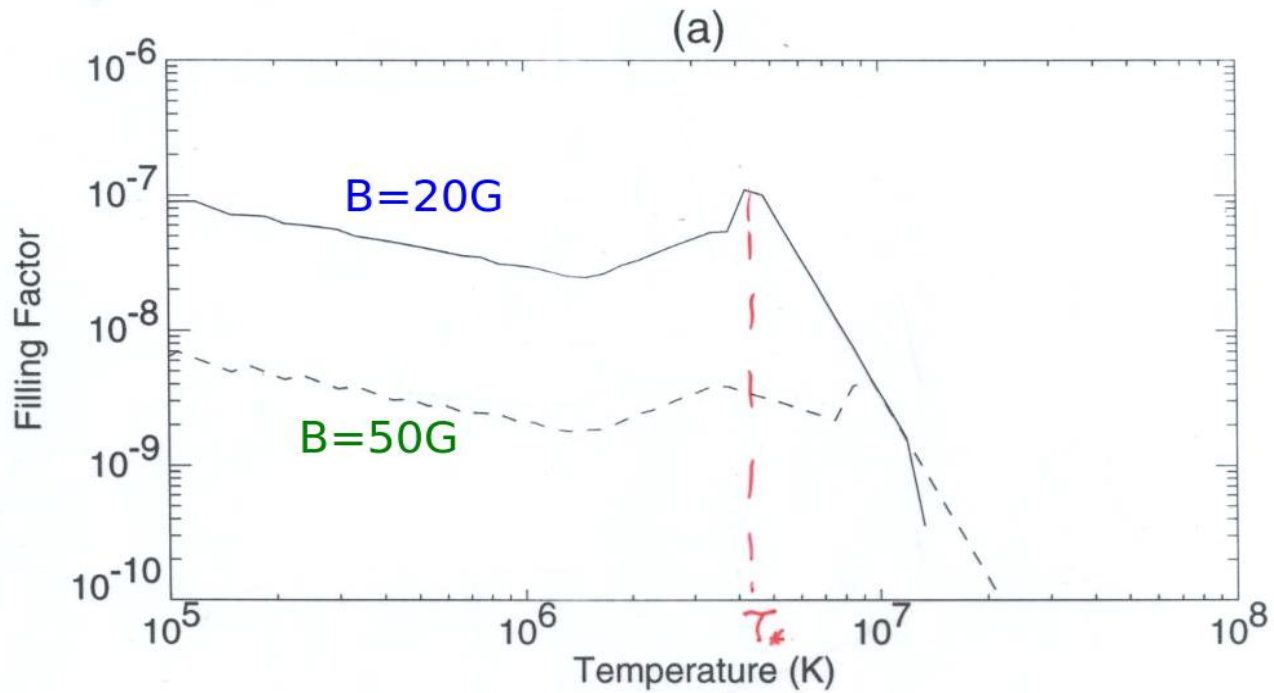
statistical steady state

chromospheric evaporation

- broad temperature and density distribution of filaments
- continuous replenishment of the coronal plasma

$t \rightarrow (\Delta t)_h$





Nanoflare-heating scaling laws

- Predicted DEM distribution
- Temperature detected by a broad-band X-ray telescope (Yohkoh SXT):

$$T \approx T_* \approx 4 \times 10^{-2} B^{2/3} L^{1/3}$$

$$B \approx (30 \div 50) \text{ G} \Rightarrow \underline{T_* \approx (4 \div 6) \times 10^6 \text{ K}}$$

- Coronal filling factor (fraction of volume filled with hot X-ray emitting plasma)

$$f \approx 2 \times 10^{-3} g / B^{2/3} L^{1/6}$$

$$f \approx (10^{-1} \div 10^{-2}) \ll 1$$

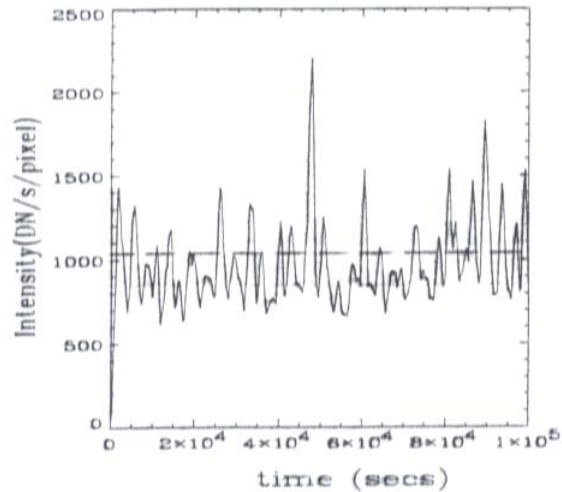
Can be obtained observationally

$$f = \frac{\langle n \rangle^2}{n_{\text{act}}^2}$$

$n_{\text{act}} \Rightarrow$ actual density of emitting plasma

$\langle n \rangle \Rightarrow$ average density \Rightarrow from emission measure

Numerical simulations of the coronal X-ray emission would be detected by Yohkoh/SXT



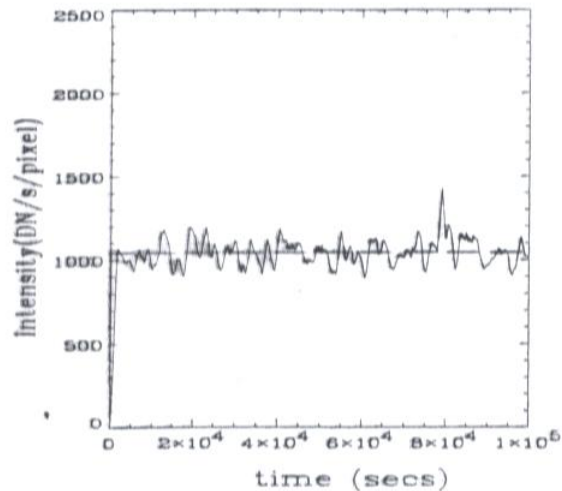
a bigger energy of nanoflares



less frequent heating events



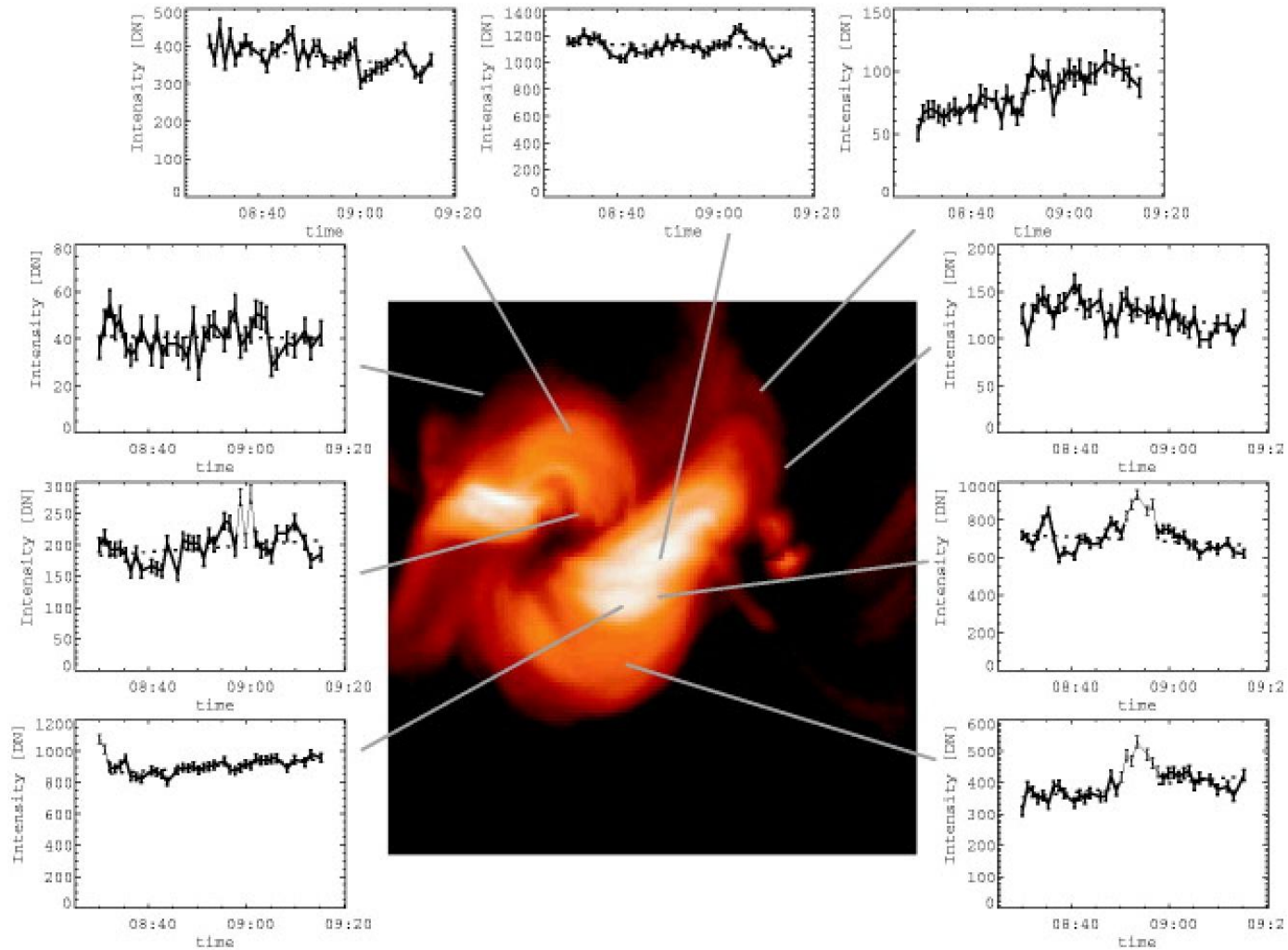
larger fluctuations



smaller nanoflares



much lower fluctuations for the same mean intensity



X-ray intensity of individual pixels from SXT (*Katsukawa & Tsuneta, 2001, ApJ*)

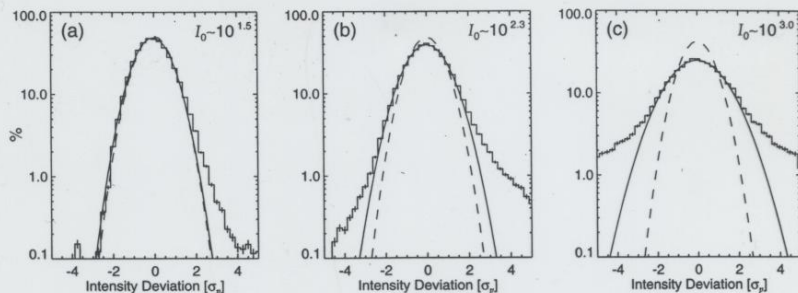


FIG. 2.—Histogram of the X-ray intensity fluctuation around the mean intensity I_0 for three intensity levels: (a) $I_0 \approx 10^{1.5}$, (b) $I_0 \approx 10^{2.3}$, and (c) $I_0 \approx 10^{3.0}$. The unit of the horizontal axis is σ_p , the standard deviation due to the photon noise. The vertical axis is the number of data points expressed as a percentage. The solid curves are the Gaussian best fitted to the core parts. The photon noise distributions are shown by dashed curves (see text).

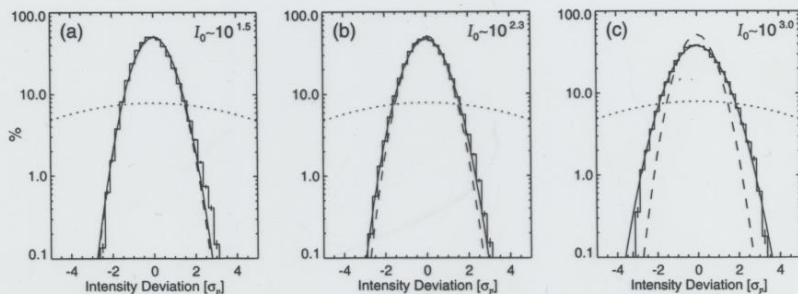
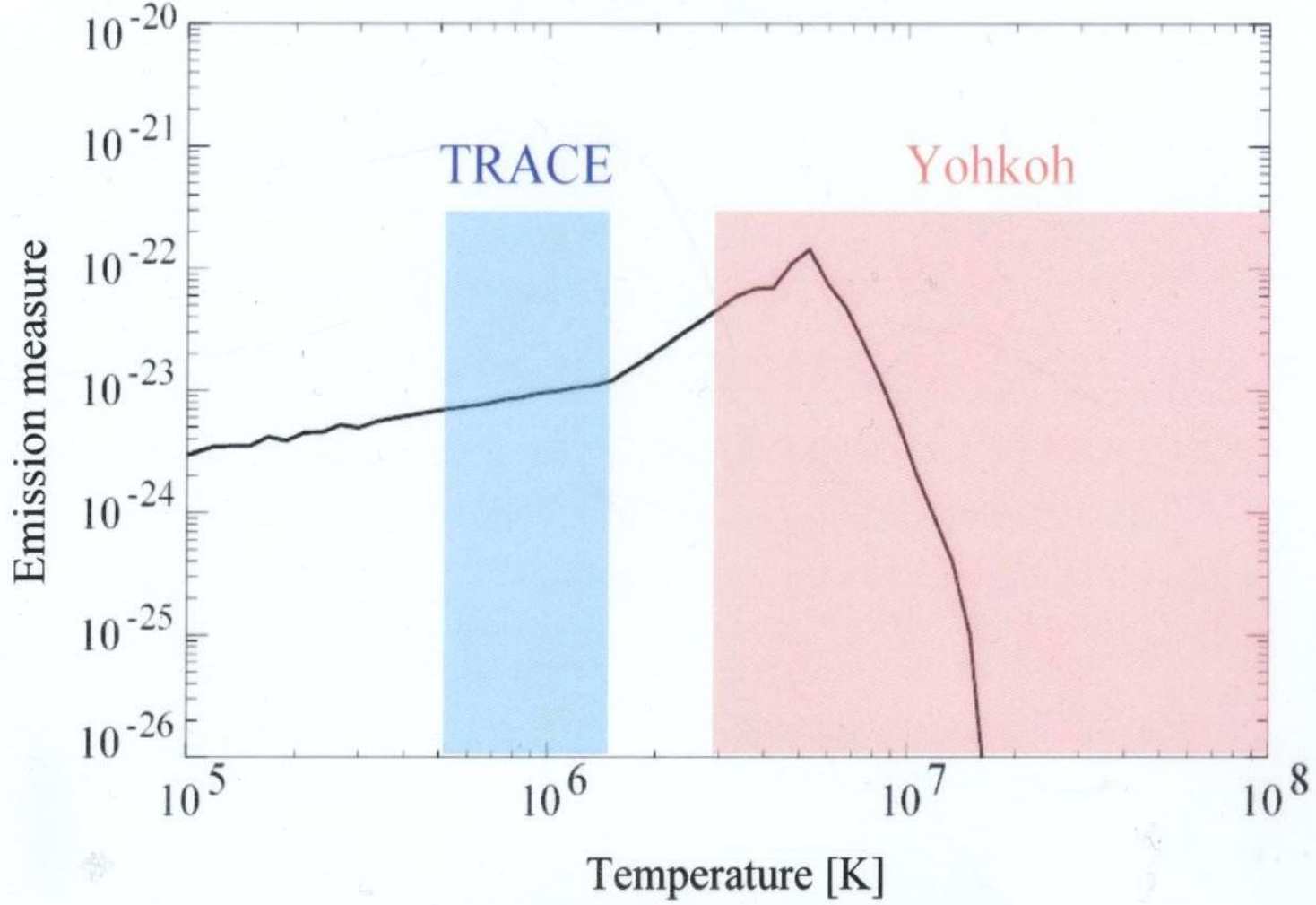


FIG. 3.—Histogram of the X-ray intensity fluctuation around the mean intensity I_0 after removing the wing component (see text). The solid curves are Gaussian best fitted to the histograms. The photon noise distributions (dashed curves) and the distribution functions for $\sigma_1/\sigma_p = 5$ (dotted curves; see text) are shown for comparison.

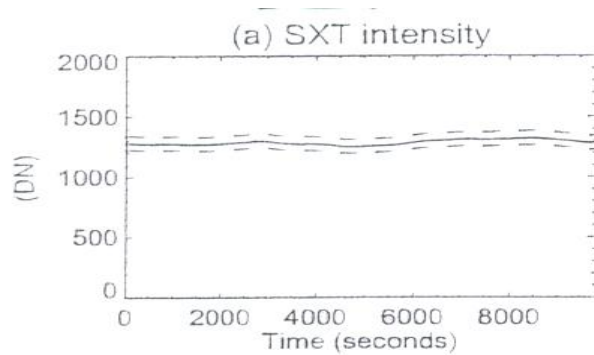
Histograms of the X-ray intensity
for different SXT pixels
(Katsurawa & Funeta, 2001)

Differential emission measure

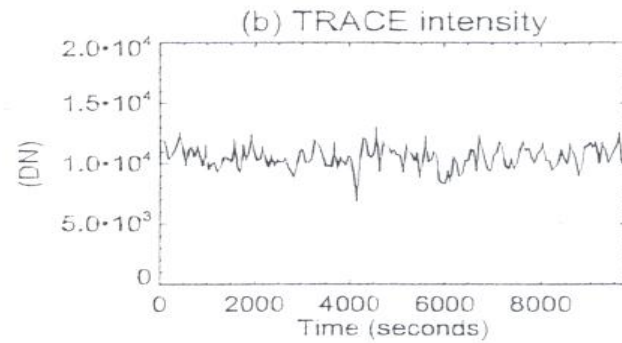


Simulated intensity variations

SXT



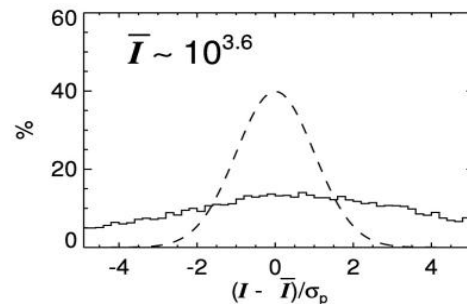
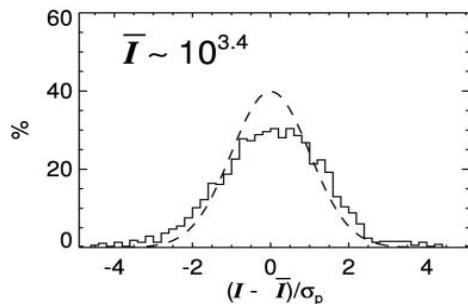
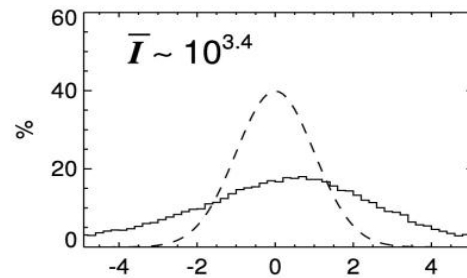
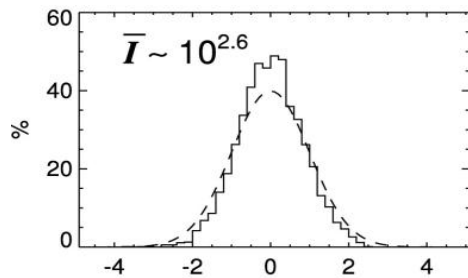
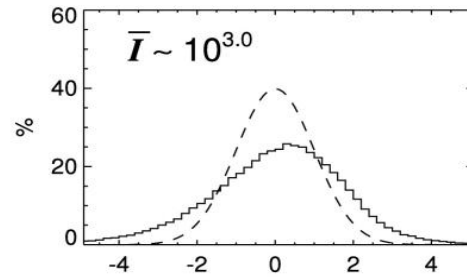
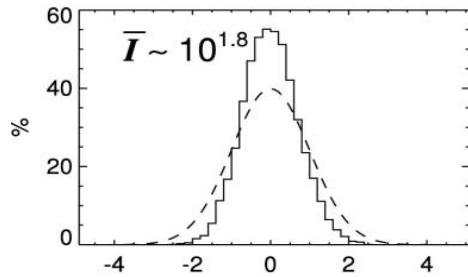
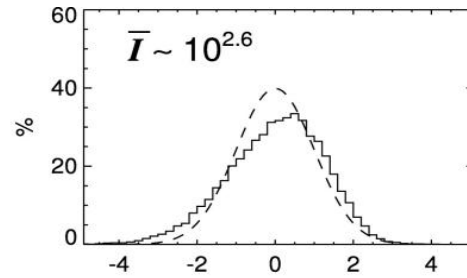
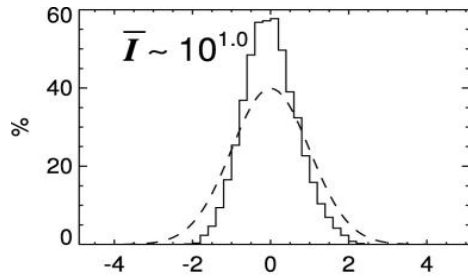
TRACE



Observed intensity variations

SXT

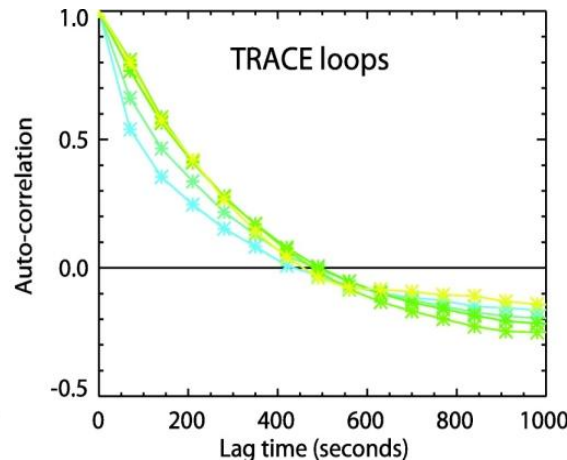
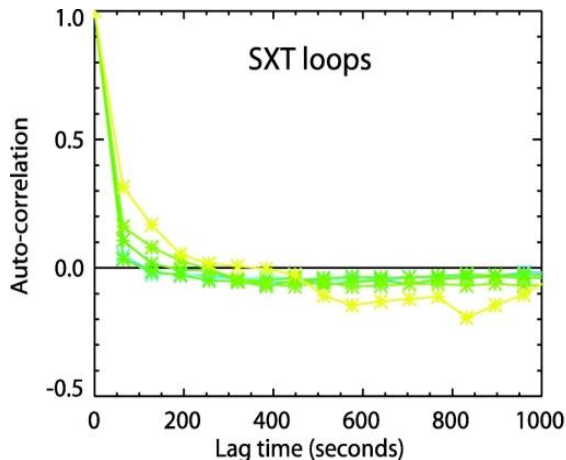
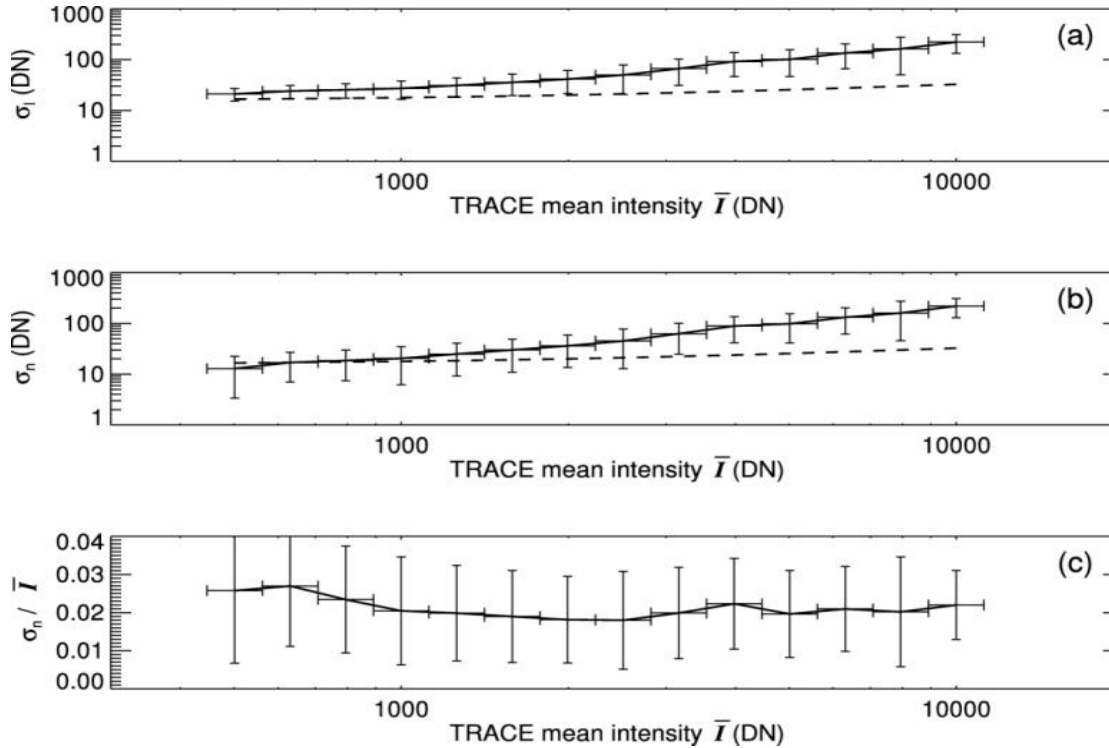
TRACE



TRACE:
detected fluctuations are well
above the estimated photon
noise
(unlike Yohkoh/SXT)

Intensity fluctuations detected by TRACE

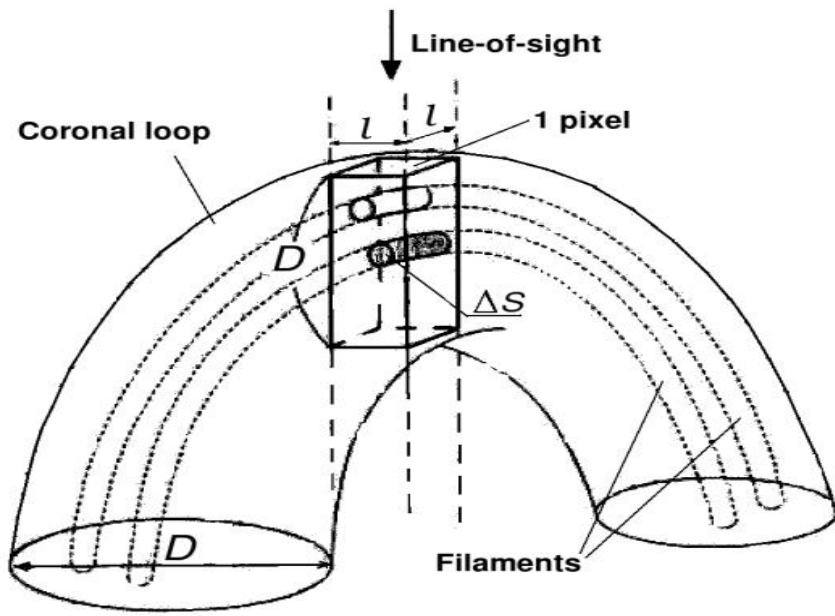
2 major characteristics:



Gaussian width:

$$\sigma_{TR} = 0.02 \langle I \rangle$$

Time-scale of fluctuations: $(\Delta t)_{TR} = 500s$



Schematic diagram:

$$L = 10^{10} \text{cm}$$

$$D = 3 \cdot 10^9 \text{cm}$$

$$l = 1.8 \cdot 10^8 \text{cm}$$

(TRACE 5x5 micropixels)

Exposure time
 $\tau_e = 27.6 \text{s}$ is much
shorter than
 $(\Delta t)_{\text{TR}} = 500 \text{s}$



Snapshot of the
instantly present
strands



$$\sigma = \langle l \rangle / \langle N \rangle^{1/2}$$

$\langle N \rangle$ - mean
number of strands
contributing to the
detected intensity



$$\sigma = 2 \cdot 10^{-2} \langle l \rangle$$

$$\langle N \rangle = 3 \cdot 10^3$$

Birth-rate of nanoflares:

$$\langle N \rangle = \frac{dN}{dt dS} (\Delta t)_{\text{TR}} D l$$

$$\frac{dN}{dt dS} = 10^{-17} \text{ cm}^{-2} \text{ s}^{-1}$$

Forward modelling



(Δt) is determined by the cooling time of relevant strands

$$(\Delta t)_{TR} = 500s$$



Radiative cooling of a plasma with $T_{TR} = 10^6 K$ and $n_{TR} = 4 \cdot 10^9 cm^{-3}$
(another way of deriving the actual density of individual strands)

“Overdense” strands: $n_{RTV} = 3 \cdot 10^8 cm^{-3}$



signature of impulsive coronal heating

The size of strands detected by TRACE and their filling factor.

$$\langle I \rangle = R_{TR} \langle N \rangle n_{TR}^2 (\Delta S) \tau_e L$$

TRACE response
coefficient

cross-section
area of a strand

Bright TRACE pixels: $\langle I \rangle_{TR} = 10^4 \rightarrow (\Delta S) = 4 \cdot 10^{12} cm^2 \rightarrow d = 20km$ across

$$\text{Filling factor: } f_{TR} = \frac{\langle N \rangle_{TR} (\Delta S)}{LD} = 2 \cdot 10^{-2}$$

Energetics of nanoflares

TRACE strand: $E_{TR} = 3 n_{TR} k T_{TR} (\Delta S) \quad 2L = 10^{23} \text{erg}$
is less than the initial energy deposition of a nanoflare E_n : **TRACE**
plasma is in the stage of radiative cooling

How to derive E_n : simultaneous SXT data

Plasma temperature detected by SXT: $T_{\text{SXT}} = 5 \cdot 10^6 \text{K}$



It relates to the peak of the DEM



$$n_{\text{SXT}} = n_{\text{RTV}} = 7 \cdot 10^9 \text{cm}^{-3}$$

Radiative cooling from $T_{SXT} = 5 \cdot 10^6 K$ to $T_{TR} = 10^6 K$

Plasma draining from $n_{SXT} = 7 \cdot 10^9 cm^{-3}$ to $n_{TR} = 4 \cdot 10^9 cm^{-3}$



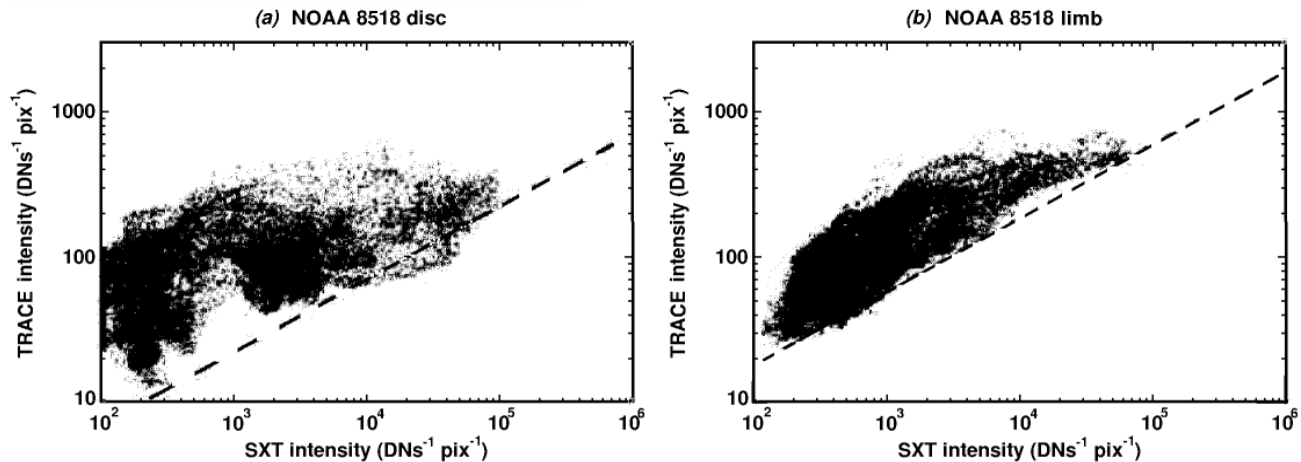
$n \sim T^{0.35}$ - very close to 1D simulations

Nanoflare energy $E_n = 5 n_{SXT} kT_{SXT} (\Delta S) 2L = 2 \cdot 10^{24} erg$

Overall energy budgett $G = En \frac{dN}{dt dS} = 2 \cdot 10^7 erg cm^{-2} s^{-1}$

Observational support

Correlation between TRACE and SXT data



Do the numbers match?

Bright TRACE pixels: $\langle I \rangle_{TR} = 10^4 \rightarrow \langle I' \rangle_{TR} = 360$



The respective SXT pixels: $\langle I \rangle_{SXT} = 3 \cdot 10^3 \dots 10^4$ ($\tau_e = 0.95s$)

On the other hands $\langle \Delta t \rangle_{SXT} = 3 \cdot 10^6 s = 6 \langle \Delta t \rangle_{TR}$



$$f_{SXT} = 6 f_{TR} \approx 0.1$$

$$\langle I \rangle_{SXT} = R_{SXT} n_{SXT}^2 l^2 D f_{SXT} \tau_e = 2 \cdot 10^3$$



... pretty consistent with the observed X-ray emission